

Exploring of structural, electronic, and optical properties of transition metal doped C₂₀ clusters

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Abstract:

In the current investigation, computational viewpoint of doped C₂₀ nano-cage with Zn, Cu⁺, Ni²⁺, and Co³⁺ was described at B3LYP*/6-311G(d,p) level of theory in singlet spin state. Vibrational analysis was established retaining of the optimized nano-cage of the minimum potential energy curve. M-C bond lengths, electronic spatial extent (ESE), photoelectron spectrum (PES) and the results of molecular orbital analysis of the studied clusters were reported. QTAIM results were considered to exploration of metal-carbon bonds characters. NICS values were provided to illustration of aromaticity the clusters. Also, doping outcome on the linear and nonlinear optical properties the clusters was demonstrated.

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Keywords: C₂₀ cluster; Electronic Spatial Extent (ESE); NICS; Photoelectron spectrum (PES); Polarizability

1. Introduction

C₂₀ cluster is considered as familiar smallest fullerene is. Preparation and characteristics of this nano-cage have been described [1]. The exploring of the structure and properties of C₂₀ cluster has been described in the various researches [2–11]. The prominent construction of C₂₀ has been involved the kindnesses of investigators [12, 13].

Nano-clusters play significant role in drug delivery systems [14], then, C₂₀ cluster and various anticancer drugs interactions examined. For instance, a computational study of solvent effect on the interaction between the cisplatin and C₂₀ informed [15]. In further research, complexation of C₂₀ and M⁺@C₂₀ (M⁺ = Li, Na, K) clusters with titanocene dichloride (TDC) reported [16].

Moreover, computational researches of interaction C₂₀ cluster with organometallic fragments have been explored structures and properties of these complexes. In a research, quantum mechanics study interaction of C₂₀ cage with Cr(CO)₅ fragment was reported [17]. In further studies, the interactions of C₂₀ cluster with diazene [18] and substituted-diazenes molecules [19] demonstrated.

In the current research, doping effect is explored in the C₂₀

clusters with Zn, Cu⁺, Ni²⁺, and Co³⁺ cations. Structural parameters, electronic properties, photoelectron spectrum (PES) and aromaticity of the clusters are reported.

2. Computational Methods

Optimizations of the studied molecules were done with the Gaussian 09 package [20]. Our calculations were considered with the B3LYP* method with c3 = 0.15 [21, 22] and the standard 6-311G(d,p) basis set [23–26]. Also, single point calculations were done on the optimized clusters at the PBE1PBE/6-311G(d,p) level of theory. This hybrid functional includes 25% exchange and 75% correlation weighting [27]. The Perdew-Burke-Ernzerhof exchange-correlation functional (PBE) is a very popular non-empirical generalized-gradient approximation (GGA).

Next outcome stationary points, their characteristics as an energy minimum were established using vibrational analysis.

Polarizability and hyperpolarizability values were computed by Multiwfn 3.8 package [28, 29]. The total static first hyperpolarizability (β_{tot}) was calculated from the following formula:

$$\beta_{\text{tot}} = \sqrt{\beta_x^2 + \beta_y^2 + \beta_z^2}$$

Where:

$$\beta_i = \beta_{iii} + \frac{1}{3} \sum_{i \neq j} (\beta_{ijj} + \beta_{ji} + \beta_{jj})$$

The Kleinman symmetry show that [30]:

$$\beta_{xy} = \beta_{yx} = \beta_{yy}; \beta_{yz} = \beta_{zy} = \beta_{zz}, \dots$$

Hence:

$$\beta_{\text{tot}} = \sqrt{(\beta_{xxx} + \beta_{xxy} + \beta_{xz})^2 + (\beta_{yyy} + \beta_{yzz} + \beta_{yx})^2 + (\beta_{zzz} + \beta_{zxy} + \beta_{zy})^2}$$

The results of quantum theory of atoms in molecules (QTAIM) analysis and picturing of the photoelectron spectrum (PES) were given with Multiwfn 3.8 package [28, 29]. The nucleus independent chemical shift (NICS) was provided to elucidate the aromaticity from the magnetic feature. NICS is demarcated as the negative value of the absolute magnetic shielding determined at the ring center [31] or extra suitable point of the structure [32].

3. Results and discussion

3.1 Energetic aspects

C_{20} cluster contains Ih point group. Doped clusters of this cluster with Zn, Cu⁺, Ni²⁺, and Co³⁺ cations reduces its point group to C_{3v} . Optimization of these doped clusters are considered B3LYP*/6-311G(d,p) level of theory in singlet spin state. Figure 1 presents optimized geometries of $[C_{19}\text{Zn}]$, $[C_{19}\text{Cu}]^+$, $[C_{19}\text{Ni}]^{2+}$, and $[C_{19}\text{Co}]^{3+}$ clusters.

Vibrational analysis of these nano-cages confirms the full-optimized geometries $[C_{19}\text{Zn}]$, $[C_{19}\text{Ni}]^{2+}$, and $[C_{19}\text{Co}]^{3+}$ reveal any imaginary frequencies, illustrative that they are placed on actual minima in the potential surface. C_{3v} geometry of $[C_{19}\text{Cu}]^+$ cage specifies an imaginary frequency at -309.00 cm^{-1} . So, this geometry is a transition state. Performance additional calculation changes this geometry to the most stable isomer. This geometry is more stable than C_{3v} -isomer (2.01 kcal/mol). This states the prominence of the geometrical fit for manipulative stable

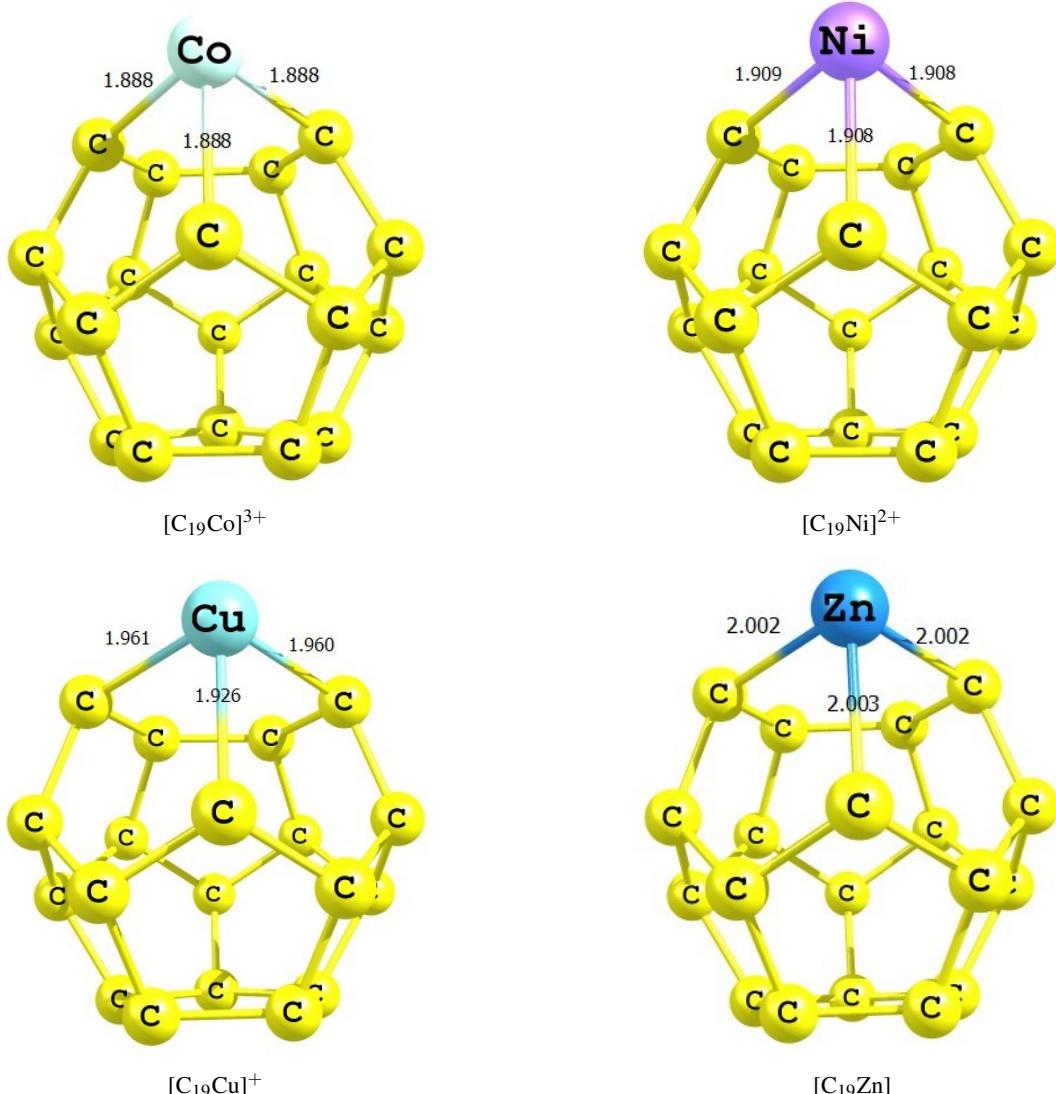


Figure 1. Optimized geometries and M-C bond lengths of $[C_{19}\text{Co}]^{3+}$, $[C_{19}\text{Ni}]^{2+}$, $[C_{19}\text{Cu}]^+$, $[C_{19}\text{Zn}]$ molecules at B3LYP*/6-311G(d,p) level of theory in singlet state.

clusters.

3.2 Ionization potential and electron affinity

Vertical electron affinity (EA_v) and vertical ionization potential (IP_v) of the studied clusters are provided (Table 1). It can be deduced, EA_v and IP_v values decrease as: Co > Ni > Cu > Zn. Consequently, these parameters enhance with decreasing of metal atomic number (Z_M). It is clearly to appreciate that the smaller EA_v values than those of the IP_v , identifying that these clusters can positively accept electrons. Thus, these clusters can performance as the electrophilic reagents in the chemical reactions.

3.3 Polarity

Calculated dipole moments of the studied clusters are gathered in Table 1. These values display that $[C_{19}Co]^{3+}$ cluster is non-polar, although other clusters are polar. $[C_{19}Zn]$ cluster tells most polarity between considered clusters.

3.4 Electronic spatial extent (ESE)

ESE is a physical property taking a single number (in atomic unit) defines the size of the molecule. ESE is calculated as the anticipation value of the electron density times the distance from the center of mass of a molecule. More, it is characteristics physical property of the electron density volume around the molecule. As the extent value enhances as electron cloud becomes more defused. In this case, computed ESE value of C_{20} cluster is 2074.95 a.u., however larger values have been found in the doped clusters (Table 1).

3.5 Bond distances

Metal-carbon bond distances of the studied clusters are presented in Figure 1. It can be detected M-C bond distances decrease as: Zn > Cu > Ni > Co. These bond lengths are similar M-C bond distances in the alkyl-transition metal complexes [33–36]. Equal M-C bonds are found in the presence of Zn, Ni^{2+} , and Co^{3+} . Nonetheless, in the presence of Cu^+ cation one of the Cu-C bond is shorter than two other bonds. These bond lengths variations are attributed to Jahn-Teller distortion in this cluster.

3.6 QTAIM

The outcomes of QTAIM analyses are valuable to exploring of metal-carbon bonds in the investigated clusters. Computed electron density at three bond critical point of metal-carbon bonds (ρ BCP) are 0.1375 ($M=Co^{3+}$), 0.1267 ($M=Ni^{2+}$), and 0.0943 ($M=Zn$) $e.\text{\AA}^{-3}$. Computed ρ BCP values of two Cu-C bonds are 0.1046 $e.\text{\AA}^{-3}$ and other bond is 0.11589 $e.\text{\AA}^{-3}$. It can be deduced, average of ρ BCP values for three bonds reduce with enhancing of Z_M . Thus, the trend of M-C bond strength alterations as: Zn < Cu < Ni < Co.

Computed Laplacian of electron density at three bond critical point of metal-carbon bonds ($\nabla^2\rho$ BCP) are 0.1826 ($M=Co^{3+}$), 0.1111 (Ni^{2+}), and 0.2232 (Zn) $e.\text{\AA}^{-5}$. Computed $\nabla^2\rho$ BCP values of two Cu-C bonds are 0.2105 $e.\text{\AA}^{-5}$ and other bond is 0.1448 $e.\text{\AA}^{-5}$.

Computed density energy (HBCP) at three bond critical point of metal-carbon bonds are -0.0559 (Co^{3+}), -0.0520 (Ni^{2+}), and -0.0332 (Zn) $e^2.\text{\AA}^{-4}$. Computed HBCP values of two Cu-C bonds are -0.0389 $e^2.\text{\AA}^{-4}$ and other bond is -0.0465 $e^2.\text{\AA}^{-4}$.

Computed potential density energy (V_{BCP}) at three bond critical point of metal-carbon bonds are -0.1574 ($M=Co^{3+}$), -0.1318 ($M=Ni^{2+}$), and -0.1221 ($M=Zn$) $e^2.\text{\AA}^{-4}$. Compute V_{BCP} values of two Cu-C bonds are -0.1299 $e^2.\text{\AA}^{-4}$ and other bond is -0.1293 $e^2.\text{\AA}^{-4}$.

Positive $\nabla^2\rho$ BCP and negative HBCP at BCP(M-C) bonds tell that the metal-carbon bonds be classified to intermediate bonds between covalent and ionic bonds. Similar arrangement is found in organometallic compounds.

3.7 Molecular orbital analysis

Figure 2 exhibits plots of frontier orbitals of the studied clusters. Results of this analysis are shown in Table 2. It can be observed; larger E(HOMO) and E(LUMO) with enhancing of Z_M . Thus, stability of HOMO and LUMO reduce with enhancing of Z_M . On the other hand, computed HOMO-LUMO gap values variate as Zn > Cu > Ni > Co. Accordingly, $C_{19}Zn$ cluster reveal the most electrical conductivity. Calculated chemical potential values rise with enhancing of atomic metal number. Electrophilicity values of the clusters enhance as Co < Ni < Cu < Zn. Then, the functional influences on the frontier orbital energy and HOMO-LUMO gap values are provided. Results

Table 1. Vertical ionization potential (IP_v , eV), vertical electron affinity (EA_v , eV), dipole moment (μ , Debye) electronic spatial extent (ESE, a.u.), NICS (ppm) values of $[C_{19}Co]^{3+}$, $[C_{19}Ni]^{2+}$, $[C_{19}Cu]^+$, $[C_{19}Zn]$ molecules at B3LYP*/6-311G(d,p) level of theory.

Cluster	IP_v	EA_v	μ	ESE	NICS
C_{20}	6.83	1.49	0.00	2074.95	-19.77
$C_{19}Co^{3+}$	22.28	16.43	0.05	2533.15	-33.52
$C_{19}Ni^{2+}$	16.49	11.48	2.34	2590.83	-34.44
$C_{19}Cu^+$	12.06	6.92	1.52	2668.79	-34.46
$C_{19}Zn$	7.45	1.29	3.10	2752.30	-45.99

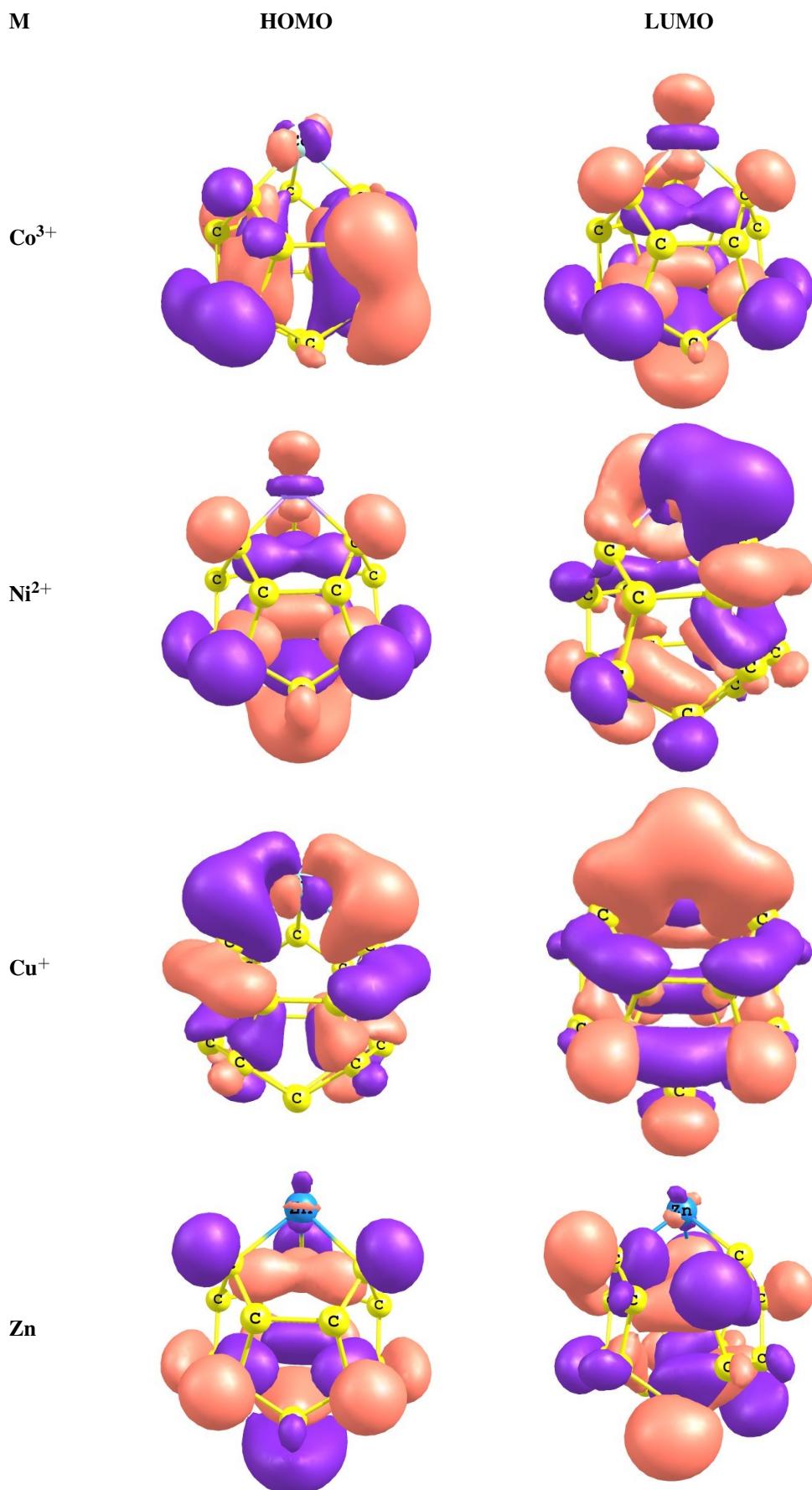


Figure 2. Plots of frontier orbitals of the $[\text{C}_{19}\text{Co}]^{3+}$, $[\text{C}_{19}\text{Ni}]^{2+}$, $[\text{C}_{19}\text{Cu}]^+$, $[\text{C}_{19}\text{Zn}]$ molecules.

of calculations of single point on the optimized clusters at the PBE1PBE/6-311G(d,p) level of theory are listed in Table 2. It can be found, identical variations of E(HOMO), E(LUMO) and gap values at two level of theory.

3.8 Photoelectron spectroscopy

Theoretical photoelectron spectra (PES) of the investigated clusters are shown in Figure 3. These spectra are constructed on generalized Koopmans' theorem. It can be inferred that the initial peaks are seemed at 5.71, 12.06, 16.49, and 22.28, eV in the $[C_{19}Zn]$, $[C_{19}Cu]^+$, $[C_{19}Ni]^{3+}$ and $[C_{19}Co]^{3+}$ clusters, respectively. It basically inferred first ionization potential values enhance as: Zn < Cu < Ni < Co.

Table 2. Frontier orbital energy, HOMO-LUMO gap, chemical potential (μ) and electrophilicity (ω) values (in eV) $[C_{19}Co]^{3+}$, $[C_{19}Ni]^{2+}$, $[C_{19}Cu]^+$, $[C_{19}Zn]$ molecules at (a)B3LYP*/6-311G(d,p) (b) B3LYP*/6-311G(d,p)//PBE1PBE/6311G(d,p) level of theory.

Cluster	level a			Level b				
	E(HOMO)	E(LUMO)	Gap	μ	ω	E(HOMO)	E(LUMO)	Gap
$C_{19}Co^{3+}$	-20.28	-18.31	1.98	-19.30	188.32	-21.00	-18.53	2.47
$C_{19}Ni^{2+}$	-14.67	-13.26	1.41	-13.97	138.03	-15.43	-13.42	2.01
$C_{19}Cu^+$	-10.11	-8.73	1.39	-9.42	64.04	-10.98	-8.93	2.06
$C_{19}Zn$	-5.71	-3.07	2.64	-4.39	7.30	-6.43	-3.20	3.22

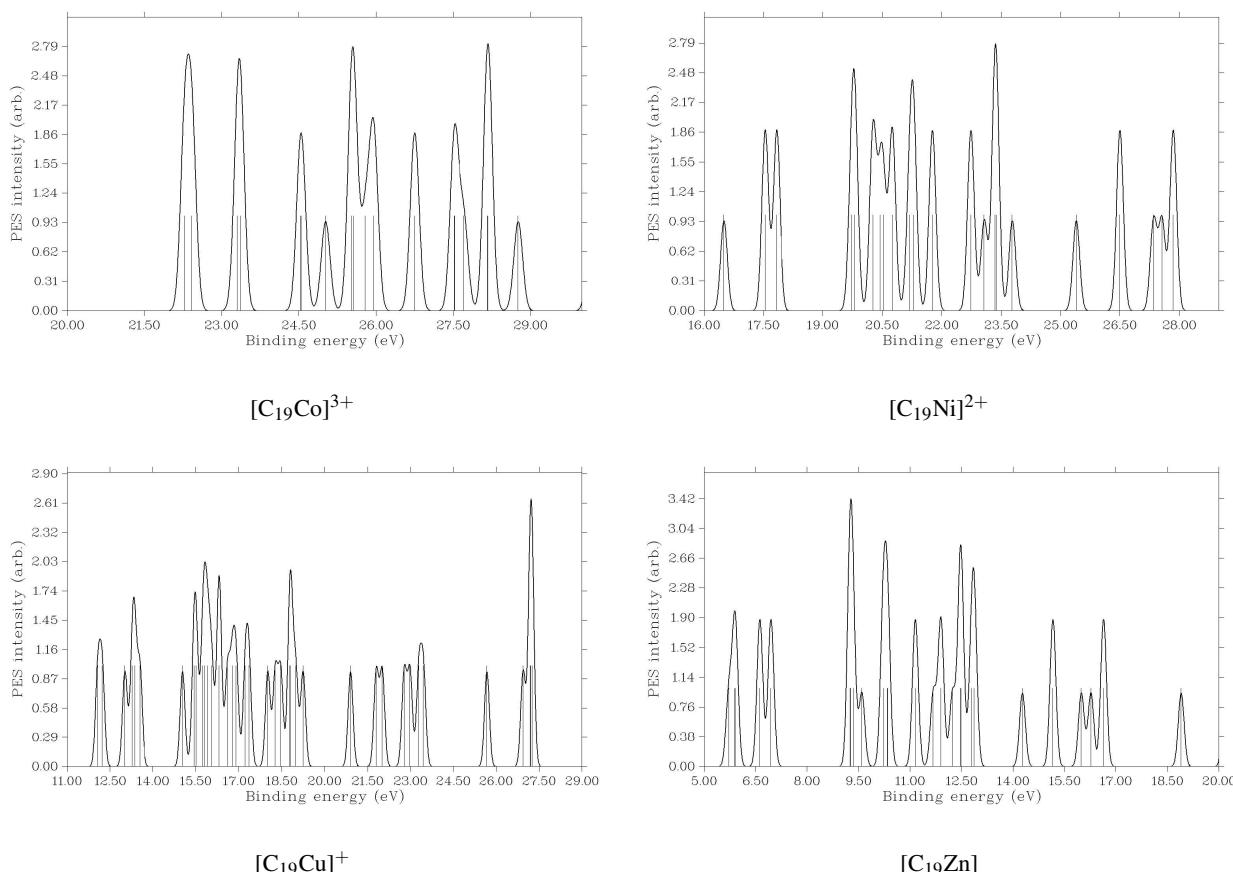


Figure 3. Photoelectron spectra of $[C_{19}Co]^{3+}$, $[C_{19}Ni]^{2+}$, $[C_{19}Cu]^+$, $[C_{19}Zn]$ clusters.

3.9 Aromaticity

NICS data are valuable information about aromaticity in the various systems [37–50]. NICS values of C_{20} and $[C_{19}M]^n$ clusters are computed to illustration of aromaticity in these systems (Table 1). Negative NICS values reveal aromaticity character of these clusters. It can be immediately know larger aromaticity in $[C_{19}M]^n$ clusters than C_{20} cluster. Aromaticity of clusters has been increased with enhancing of Z_M . Therefore, aromaticity of clusters increases with increasing of Z_M .

3.10 Polarizability

α_{iso} data (static isotropic polarizability) of the C_{20} and $[C_{19}M]^n$ clusters are included in Table 3. It immediately

Table 3. Static isotropic polarizabilities values (α_{iso} , a.u.), static first hyperpolarizability values (β_{tot} , a.u.), dynamic polarizability ($\alpha(-\omega; \omega)$, a.u.), dynamic first hyperpolarizability values ($\beta(-2\omega; \omega, \omega)$, a.u.), scattering hyperpolarizability (β_{HRS} in a.u.) of $[\text{C}_{19}\text{Co}]^{3+}$, $[\text{C}_{19}\text{Ni}]^{2+}$, $[\text{C}_{19}\text{Cu}]^+$, $[\text{C}_{19}\text{Zn}]$ molecules at $w = 0.065600$ (694.56 nm) at B3LYP*/6-311G(d,p) level of theory.

Cluster	α_{iso}	β_{tot}	$\alpha(-\omega; \omega)$	$\beta(-2\omega; \omega, \omega)$
$[\text{C}_{19}\text{Co}]^{3+}$	164.81	89.03	171.35	1806.29
$[\text{C}_{19}\text{Ni}]^{2+}$	172.01	575.32	186.83	774.44
$[\text{C}_{19}\text{Cu}]^+$	179.69	449.43	201.93	2322.73
$[\text{C}_{19}\text{Zn}]$	186.85	1121.60	204.75	833.03

knows larger α_{iso} values with enhancing of Z_M . These computed parameters make evident linear optical properties of clusters, and the attendance of polarizabilities is owed to asymmetric electronic density distribution in these clusters. Dynamic polarizabilities are given from frequency-dependent polarizability. In this work, the incident-frequency (ω) effect on the first polarizability is considered at applied frequencies of 694.56 nm. Direct current second harmonic generation (DCSHG) is employed to calculation of the frequency-dependent polarizability $\alpha(\omega)$. Compute polarizability data ($\alpha_{\text{iso}}(-\omega; \omega)$) corresponding to 694.56 nm incident light for the investigated clusters are listed in Table 3. It can be observed, $\alpha_{\text{iso}}(-\omega; \omega)$ values decrease as: Zn > Cu > Ni > Co. The similar trend finds in the isotropic polarizability variations.

3.11 Hyperpolarizability

β_{tot} values (static first hyperpolarizability) of the investigated clusters are evaluated (Table 3). $[\text{C}_{19}\text{Zn}]$ cluster reveals largest β_{tot} value. It must be noticed that electronic properties notably influence to hyperpolarizability response, and the more variants in dipole moment give the higher hyperpolarizabilities parameters.

The incident-frequency (ω) effect is revealed on the β_{tot} data at applied frequencies of 694.56 nm. $\beta(\omega)$ values (frequency-dependent first hyperpolarizability) are computed with DCSHG.

Frequency-dependent first hyperpolarizability would advise supportive data for judging dynamic first hyperpolarizability. The first hyperpolarizability data ($\beta(-2\omega; \omega, \omega)$) corresponding to $w = 0.065600$ (694.56 nm) incident light are estimated for the investigated clusters (Table 3). $[\text{C}_{19}\text{Cu}]^+$ cluster indicates largest $\beta(-2\omega; \omega, \omega)$ value.

4. Conclusion

Doping of C_{20} cluster with Zn, Cu^+ , Ni^{2+} , and Co^{3+} cations at B3LYP*/6-311g(d,p) level of theory in illustrated C_{3v} point group for optimized structure of $[\text{C}_{19}\text{Zn}]$, $[\text{C}_{19}\text{Ni}]^{2+}$ and $[\text{C}_{19}\text{Co}]^{3+}$ clusters. In contrast, $[\text{C}_{19}\text{Cu}]^+$ cluster distorted from C_{3v} symmetry. Equal metal carbon bond lengths were found for Zn, Ni and Co. but, two of the Cu-C was longer than other bond in $[\text{C}_{19}\text{Cu}]^+$ cluster. Aromaticity of clusters reduced with decreasing of Z_M . Computed α_{iso} and $\alpha_{\text{iso}}(-\omega; \omega)$ values enhanced with increasing of Z_M . $[\text{C}_{19}\text{Zn}]$ and $[\text{C}_{19}\text{Cu}]^+$ clusters revealed largest β_{tot} and

$\beta(-2\omega; \omega, \omega)$ values, respectively.

Authors Contributions

All authors have contributed equally to prepare the paper.

Availability of Data and Materials

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Conflict of Interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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