







Numerical analysis of fluid flow behavior in micro fracture of coal matrix

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Abstract:

Coal beds are very complex porous media that exhibit heterogeneity, dual-porosity, and stress sensitivity. Simulation models for fluid flow from coal matrix for coal bed methane (CBM) and enhanced coal bed methane (ECBM) recovery have significantly progressed in recent decades. Analytical models have limitations or challenges in application due to assumptions and oversimplification. Therefore, in this study, numerical modeling and simulations were carried out to investigate the fluid flow behavior in the microchannel of the coal matrix. A variation in pressure drop was considered to evaluate the flow pattern in the coal matrix. Analysis was carried out to assess the effect of pressure drop on fluid velocity in the microchannel. The results of the simulations indicated an increased fluid velocity with pressure drop. Well-developed and connected microchannel was significant for transporting fluid in the coal matrix. The Simulation results were found helpful in estimating the critical pressure drop to enhance fluid flow in the microchannel of the coal matrix.

Keywords: Coal matrix; Microchannel; Fluid velocity; Numerical analysis

1. Introduction

The coal matrix stores the maximum amount of methane in its porous structure. The transportation of methane within the coal matrix is only possible by the proper connectivity between the pores and fracture channel. The microfracture in the coal matrix facilitates good connectivity between pores and microchannels during gas transportation. This micro and macro channel is susceptible to reservoir parameters like pressure. A decline in pore pressure raises effective stress and causes the narrowing or closer of fractures. The reduction in fracture aperture reflects the declining methane production rate during gas transportation. Therefore, a detailed study of flow patterns with pressure drop is essential to evaluate the feasibility and recovery rate in the CBM production process.

The effect of pressure depletion on the deformation of the

coal matrix and change in fracture aperture was studied elsewhere (Clarkson et al., 2010; Clarkson et al., 2013; Wei and Zhang, 2013; Kumar et al., 2017). The studies showed reduced permeability due to the narrowing and closing of the fracture aperture at lower pore pressure. An increase in adequate pressure leads to the crushing of the cleat structure. Ma et al. (2017) studied the impact of geomechanical parameters on coal beds and concluded with flow patterns during the CBM production process. A reduction in permeability with an increase in stress parameters was observed during the investigation. The decline in permeability was due to the narrowing or closure of the fracture at a higher stress value. Wang et al. (2019) studied the interaction of coal matrix with permeability at variable pressure. A reduced permeability was observed with downstream pressure. The reduction in permeability was attributed to the change in cleat structure and deformation in the coal matrix. Thus, a

variation in reservoir pressure resulted in deformation in the coal matrix, change in fracture aperture, and flow pattern in the coal matrix. Investigating changes in flow patterns with pressure at a laboratory scale is costly and time-consuming. Therefore, the analytical and numerical model is used to visualize flow patterns in coal seams at variable pressure. The researchers proposed many models to correlate the flow pattern with changes in pore pressure.

Ramanandraibe et al. (2021) developed a reservoir model to study the formation's multilayer and permeability anisotropy effects. Results were concluded with higher productivity at a lower permeability anisotropy ratio. Li and Liu (2022), Dehghan and Yazdi (2023) used Monte Carlo and Box Muller methods to determine gas flow characteristics in the coal bed. The fracture in the plastic zone was found beneficial for fluid flow in the coal bed. A decline in permeability was observed with creep deformation in fracture.

Previous studies have been carried out to determine the flow behavior in microchannels while the connectivity and flow through the microchannel are essential for the continuity of flow. Therefore, numerical modeling and simulation were carried out to study the impact of reservoir parameters on fluid flow behavior in coal beds. The fluid flow in macro fractures was studied in detail and reported elsewhere (Dabiri et al., 2017; Zhang et al., 2019; Ye et al., 2020; Yan et al., 2021). Kumar et al. (2017) used COMSOL Multiphysics to model coal deformation under fluid pressure. Results were reported with swelling in the coal matrix at elevated injection pressure. Mohanty and Pal (2016) investigated the flow characteristics in coal beds using COMSOL Multiphysics. The velocity and pressure fluctuation were determined in the coal bed under reservoir conditions (Xu et al., 2021). Studies reported the impact of reservoir parameters on the microchannel of the coal matrix during CBM production (Wei and Zhang, 2010; Fan et al., 2020). The coal matrix's microchannel is a critical feature that establishes connectivity during gas transportation. Therefore, in this research work, numerical modeling and simulation were carried out to determine the effect of pressure drop on

fluid flow in the microchannel of the coal matrix. The SEM image was used for modeling, and a continuous pressure drop was assumed for the simulation. Fluid velocity was determined to predict the flow pattern in the microchannel. The novelty of the research work is towards predicting flow patterns in the microchannel of the coal bed during the CBM production process. The results will be helpful for the prediction of fluid flow in microchannels and the estimation of production rate during the CBM exploitation.

2. Geometrical model

The scanning electron microscopic image of the coal sample obtained from Jharia Coalfield India was used for modeling (Fig. 1 a). The SEM image was converted into.DXF file. The CAD drawing file was imported into COMSOL Multiphysics 5.5 version software suit (Fig. 1 b).

2.1 Description of geometrical model

The fluid flow analysis in microfractures of the coal sample obtained from the study area was carried out using the Creeping Flow (Stokes Flow) model. The model was chosen to analyze the microfracture's stoke flow in grain nuances. The modeling was carried out to determine fluid movement through the pore geometry to the surface of the porous rock at variable pressure drops. The pore-scale flow analysis was conducted elsewhere using COMSOL Multiphysics to examine the flow pattern in the porous material (Sirivithayapakorn and Keller, 2003; Auset and Keller, 2004). The Scanning electron microscopic image of 850×900 micrometer of coal sample obtained from the study area was collected and used for the modeling purpose (Fig. 1 b). The image is first converted to.DXF file to represent the microstructure of coal matrix in drawing form and imported into the COMSOL Software suite 5.5. The imported drawing was considered a single continuum with continuous properties throughout the model. The boundary conditions for fluid transportation were applied to the coal matrix. The input and output were assigned to the upper and lower surface of the imported drawing (Fig. 2). The symmetry was given to the wall, as shown in (Fig. 3). Methane gas with

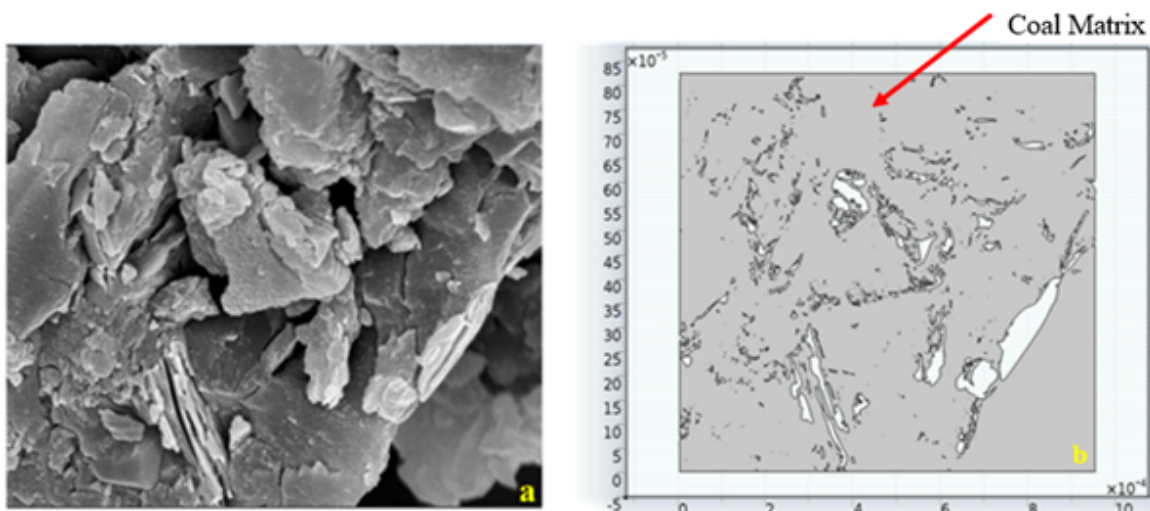


Figure 1. SEM image used for the modelling (a) SEM image of coal sample (b) SEM image converted in to .DXF format (Unit = m).

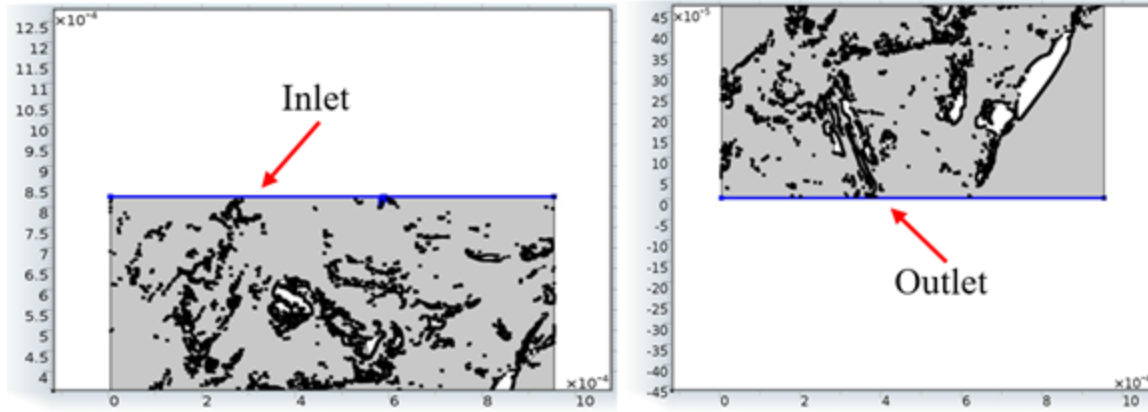


Figure 2. Assignment of Boundary condition (a) Inlet for fluid Transportation (b) Outlet for fluid Transportation.

a fluid density of 0.6038 kg/m^3 was considered to pass through the fractures. The gas was passed in such a way that it was not penetrating the solid particles. Methane was passed from inlet to outlet, and no flow zone was considered towards the symmetry.

2.2 Model definition and governing equations

The Stokes equation was considered to solve the flow of fluid in the microchannel. The equation was assumed to visualize the fluid flow pattern. Stroke equation for fluid flow in the microchannel is written as (El-Amin, 2022):

$$\mu \nabla^2 u - \nabla p = 0 \tag{1}$$

$$\nabla u = 0 \tag{2}$$

where, u = velocity of the fluid (m/s); p = pressure (Pa); μ = dynamic viscosity (Pa.s).

Force was not applied therefore it is not considered in the Equation. The explicit equation of the velocity vector is given as:

$$\mu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) - \frac{\partial p}{\partial x} = 0 \tag{3}$$

$$\mu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right) - \frac{\partial p}{\partial y} = 0 \tag{4}$$

$$\mu \left(\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) - \frac{\partial p}{\partial w} = 0 \tag{5}$$

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \tag{6}$$

If the density is assumed constant then the Eq. 1 is modified as:

$$\nabla \mu (\nabla u + \nabla u^T) - \nabla p = 0 \tag{7}$$

Brinkman equations, with the Stokes-Brinkman assumption used for the creeping flow as:

$$-\nabla p + \nabla \frac{\mu}{\epsilon_p} (\nabla u + \nabla u^T) - \frac{\mu}{k} u = 0 \tag{8}$$

where, ϵ_p is the porosity, and k is the permeability of the medium.

The porosity and permeability were calculated based on the equation as:

$$k(x,y) = \frac{k_0}{100 \times im1(x,y) + 0.1} \tag{9}$$

$$\epsilon_p(x,y) = 1 - 0.99 \times im1(x,y) \tag{10}$$

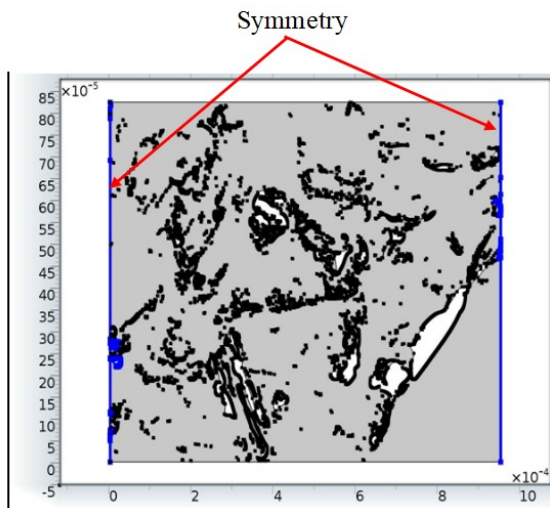


Figure 3. Assignment of symmetry into the model (dimensions are in m).

Table 1. Input Data used for Simulation.

Name	Value	Unit	Description
ρ	0.6038	kg/m^3	Fluid density
μ_0	11.77×10^{-6}	Pa.s	Dynamic viscosity
ΔP	9×10^{-4} to 21×10^{-4}	Pa	Pressure drop

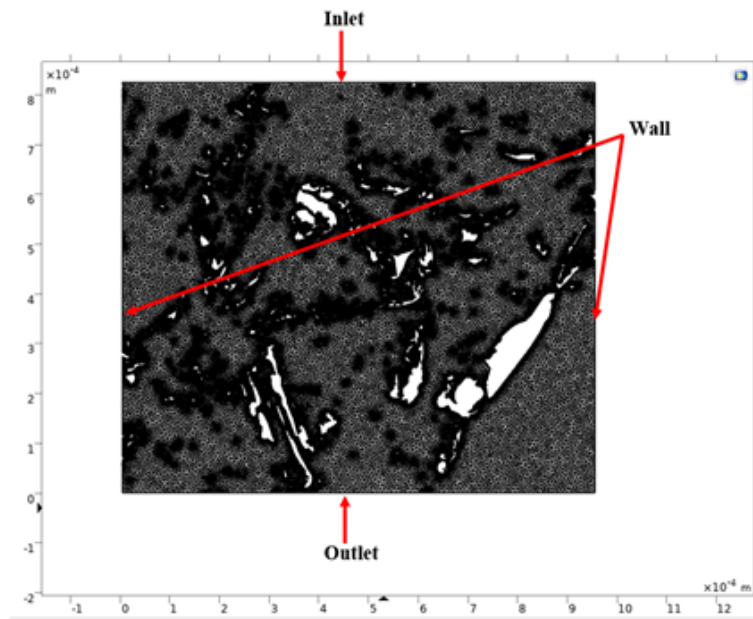


Figure 4. Meshed model for analysis.

where, $iml =$ image function. The image function was derived from the imported image and varied from 0 to 1. The model was solved at a variable pressure drop. No-slip condition was considered by keeping zero velocity at the boundary. The input data used in simulation is summarized in Table 1.

3. Meshing parameters

The model was subdivided into discrete geometrical shapes using a meshing tool. The mesh cells were used for the discrete local approximation of the complete model. Discretization was performed using a free triangular element to simplify the calculation. The parameters used for the meshing are presented in Table 2. The meshed surface is shown in (Fig. 4).

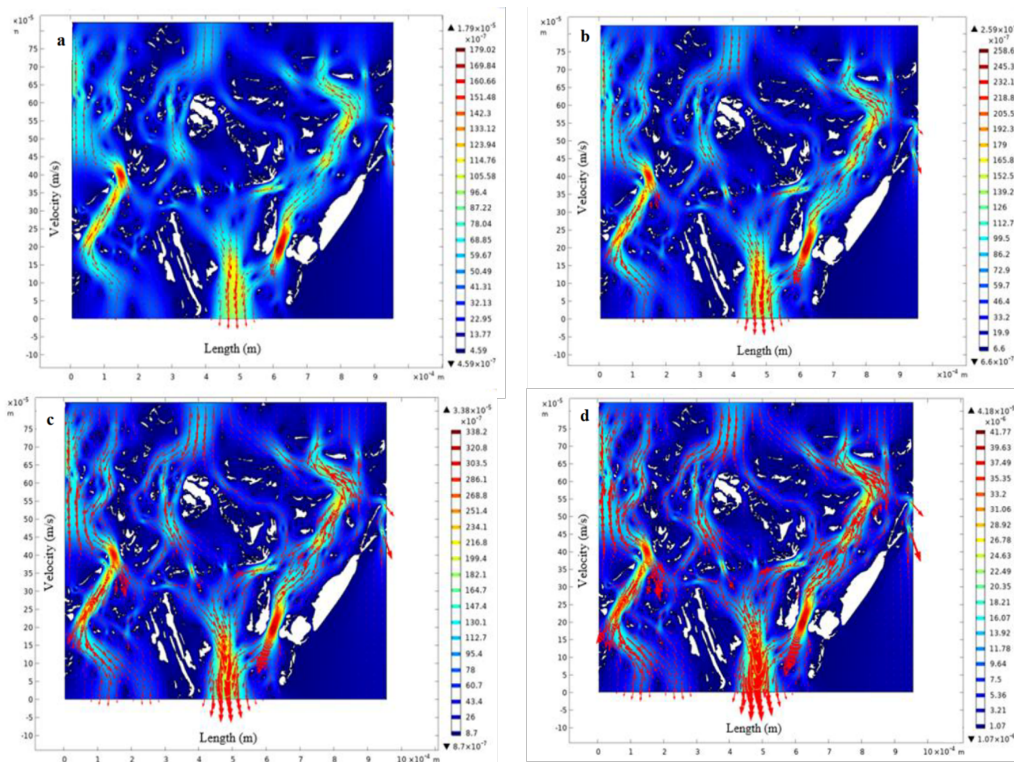


Figure 5. Velocity magnitude at variable pressure drop (a) Pressure drop at 0.000900 P*a (b) Pressure drop at 0.001300 Pa (c) Pressure drop at 0.001700 Pa (d) Pressure drop at 0.002100 Pa.

Table 2. Meshing parameters for discretization of model.

Meshing parameters	Value
Mesh quality	0.9032
Elemental type (triangular)	186577
Elements (edge)	19109
Elements (edge)	13715
Sequence type	Physics-controlled
Element size	Normal

4. Results and discussion

The simulation was carried out to solve the model according to the input parameters shown in Table 1, following the Creeping Flow (Stokes Flow) model. Pressure drop varied from 9×10^{-4} to 21×10^{-4} Pa to evaluate fluid velocity in the microchannel. An increase in pressure drops, i.e., 4×10^{-4} Pa, was used in each run. The results of the velocity profile are shown in (Fig. 5). The contour profile indicated an increase in velocity with pressure drop. Fluid velocity varied from 4.59 to 179.02×10^{-7} m/s at the pressure drop 9×10^{-4} Pa (Fig. 5 a). The developed and connected microchannel was observed with smooth and continuous flow. As the pressure drop increased to 13×10^{-4} Pa, the fluid velocity raised from 6.6 to 258.6×10^{-7} m/s, indicating an extension in fracture width (Fig. 5 b). Further increment in pressure drop from 13 to 21×10^{-4} Pa surges the fluid velocity from 8.7 to 417.7×10^{-7} Pa (Fig. 5 c and 5 d). The rise in fluid velocity with pressure drop has been attributed to the extension in fracture width and higher permeability. The correlation of fluid velocity with arc length (horizontal length) shown in Fig. 6 indicated an increase in fluid velocity with pressure drop. Higher velocity was observed at pressure drop varied from 17 to 21×10^{-4} Pa. A reduction in fluid velocity between 300 to 400 μm was due to the narrow path and cross-connections. Fluid velocity was higher because the fractures were well-

developed and connected with the coal matrix.

A well-developed microchannel in the coal matrix showed an increase in fluid velocity. The cross-extension area in the coal matrix hindered the gas flow. The arc length up to 150 μm indicated increased fluid velocity because of the well-developed and connected microchannel. Further connectivity of fractures was available at approx 400 to 800 μm . The fracture connectivity facilitates the continuity of flow. The connectivity of the microfracture was adequate for the continuity of flow in the coal matrix.

5. Conclusion

The results of numerical analysis for fluid flow behavior in the developed model of coal matrix are concluded as follows:

- Well-developed and connected microchannels facilitate the continuity of flow during gas transportation.
- An increase in fluid velocity was observed with an increase in pressure drop.
- An increase in velocity was attributed to the shrinkage in the coal matrix with an extension in fracture width and higher permeability.

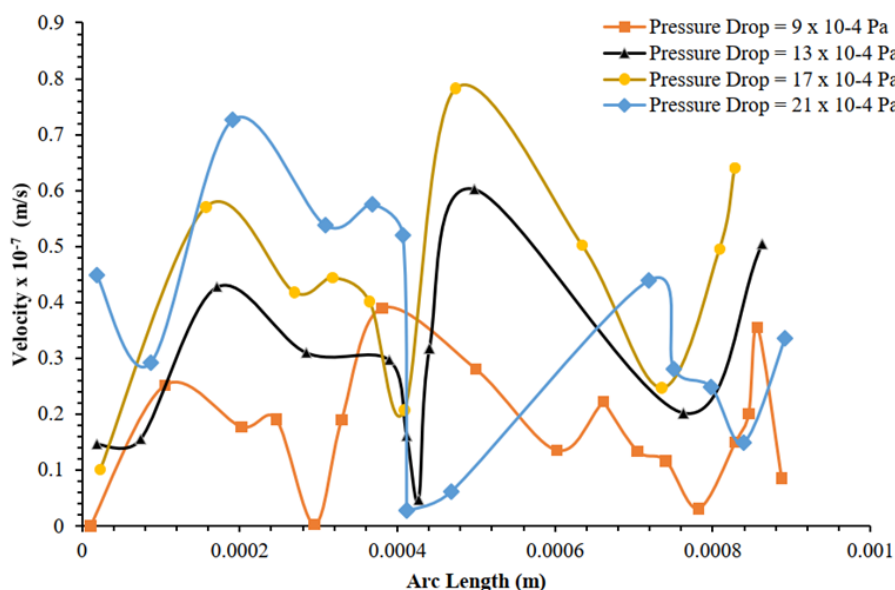


Figure 6. Correlation of fluid velocity with Arc length at variable pressure drop.

- The Cross-extension area was responsible for reducing fluid velocity in the coal matrix.
- Evaluation of critical pressure drop is essential for optimized gas transportation in the coal matrix.

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Authors contributions

All the authors have participated sufficiently in the intellectual content, conception and design of this work or the analysis and interpretation of the data (when applicable), as well as the writing of the manuscript.

Availability of data and materials

The data that support the findings of this study are available from the corresponding author, upon reasonable request.

Conflict of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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